# **ADMConstraints**

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#### Abstract

Calculate the values of the Hamiltonian and Momentum Constraints on the computational grid for output.

## 1 Physics

This analysis thorn calculates the values of the Hamiltonian and momentum constraint equations on the computational grid during a spacetime evolution. The Hamiltonian Constraint (grid function: ham) is given by

$$H = R - K^{i}{}_{i}K^{j}{}_{i} + trK^{2} - 16\pi\rho \tag{1}$$

The Momentum Constraints (grid functions momx, momy, momz) are given by

$$M_i = \nabla_i K_i^{\ j} - \nabla_i tr K - 8\pi S_i \tag{2}$$

where

$$S_i = -g_{ia}n_bT^{ab} = -g_i^a n^b T_{ab} = -\frac{1}{\alpha}(T_{i0} - \beta^j T_{ij})$$
(3)

## 2 Comments

- Symmetry boundary conditions (CactusBase/CartGrid3D) are implemented.
- Default behaviour is to apply so called flat boundary conditions to the calculated values of the constraint equations.
- Excision (Excision/LegoExcision) is included.
- The 3-metric is only included through the Macros in CactusEinstein/Einstein and as such the physical metric is used.
- Matter is included using the CalcTmuNu mechanism.
- The constraint calculation is default performed at the ANALYSIS time bin, if the constraint values are needed at every iteration, the parameter constraints\_persist should be used to schedule the calculation instead at POSTSTEP.